

## On the delay effects of different channels in Internet-based networked control systems

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The sensor-to-controller and the controller-to-actuator delays in networked control systems (NCSs) are investigated for the first time with respect to their different effects on the system performance. This study starts with identifying the delay-independent and delay-dependent control laws in NCSs, and confirms that only two delay-dependent control laws can cause different delay effects in different channels. The conditions under which the different delays in different channels can cause different effects are then given for both delay-dependent control laws. The results are verified by numerical examples. Potentially, these results can be regarded as important design principles in the practical implementation of NCSs.

**Keywords:** networked control systems; delay effects; delay-dependent control law; delay-independent control law

### 1. Introduction

Networked control systems (NCSs), i.e. control systems that are controlled over the communication network, have gained much attention in recent years. The communication network in NCSs often refers to the data network such as the Internet but not necessarily the control-oriented network such as the Control Area Network or the DeviceNet. Unlike the latter, the Internet is not designed or optimised for the control purpose, meaning that lossless data transmission as assumed in conventional control systems is not achievable for Internet-based NCSs. Therefore, despite all the potential applications of NCSs, the communication constraints in NCSs caused by the inserted communication network, i.e. network-induced delay, data packet dropout, data rate constraint, etc. have to be carefully dealt with before NCSs can be widely applied as a reliable control strategy (Xia, Liu, Shi, Rees, and Thomas 2007; Wang, Ho, Liu, and Liu 2009; Coutinho, Fu, and de Souza 2010; Jentzen, Leber, Schneisgen, Berger, and Siegmund 2010; Hua, Zheng, and Guan 2011; Zhou, Chen, Qin, Shi, and Yu 2011; Zhang and Wang 2012).

One of the most distinct characteristics among all these communication constraints is the network-induced delay, caused by the imperfect data transmission in NCSs. This is also one of the main topics in the literature on NCSs, see Zhang and Yu (2008), Lin, Wang, and Yang (2009), Meng, Lam, and Gao (2009), Wei, Wang, He, and Shu (2009). Indeed, the delay in

NCSs builds a direct bridge between the theory of NCSs and that of time-delay systems, thus enabling the latter to be widely applied to NCSs without significant difficulty. Most of these works do not distinguish between the delay in either the sensor-to-controller or the controller-to-actuator channel, meaning that the majority of the existing models of NCSs simply assume those two delays affect the system performance in the same way. Although this assumption seems naturally true, further clarifications are necessary before regarding it as a general principle: Is it universally true that the delays in both channels are identical with respect to their effects on the system performance? This question is important since, although the answer of 'yes' could confirm the correctness of existing results, the possible answer of 'no' will put all these existing results in an awkward position and open the gate for a more appropriate modelling approach to NCSs.

In order to answer the above question, we first define how the system performance in terms of different delays in different channels is measured, which turns to be entirely dependent on the choice of the control laws. We then divide the existing control laws in NCSs into two categories, that is, delay-independent (Wang and Yang 2007; Gao, Chen, and Lam 2008; Xiong and Lam 2009) and delay-dependent control laws (Liu, Xia, Rees, and Hu 2007; Zhao, Liu, and Rees 2008a,b, 2009a,b, 2010). The difference between these two categories is that the feedback gain of the former does not depend on specific delays

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while the latter does. Delay-independent control laws are often seen in most existing works on NCSs due to the simplicity of its control structure, whereas the implementation of delay-dependent control laws requires particular system setups where the packet-based control approach is one of the most efficient of its kind. After categorising the control laws the delay effects are then investigated using both qualitative and quantitative methods. Note that for ease of theoretical difficulties, we have constrained our discussions to linear systems with static state feedback. Based on the simplification, we have found meaningful results, which unfortunately suggest the necessity of a thorough reinvestigation of all the existing results aforementioned on NCSs.

The remainder of this article is organised as follows. The problem is formulated in Section 2. Existing control laws are then categorised in Section 3. The delay effects with respect to different categories of control laws are analysed both qualitatively and quantitatively in Section 4. The obtained results are verified by numerical examples in Section 5 and Section 6 concludes this article.

**Notations:** For clarity of presentations, we list some often-used notations here and the others are defined in the context where they are. The sensor-to-controller delay, the controller-to-actuator delay and the round trip delay at time  $k$  are denoted by  $\tau_{sc,k}$ ,  $\tau_{ca,k}$  and  $\tau_k := \tau_{sc,k} + \tau_{ca,k}$ , respectively. Their corresponding upper bounds are denoted by  $\bar{\tau}_{sc}$ ,  $\bar{\tau}_{ca}$  and  $\bar{\tau} := \bar{\tau}_{sc} + \bar{\tau}_{ca}$ , respectively. For simplicity of notations we also use the following simplifications where appropriate  $\alpha := \tau_{sc,k}$ ,  $\beta := \tau_{ca,k}$ , and  $\tau := \tau_k$ . The symbol  $\hat{\cdot}$  is placed on the top of a parameter to denote the estimated or predicted value of the parameter.  $u(t_1|t_2)$  where  $t_1$  is the current time instant and  $t_2$  is a previous time instant is used to denote the fact that the value  $u(\cdot)$  at time  $t_1$  is estimated or predicted based on its previous value at time  $t_2$ .

## 2. Problem formulation

The first difficulty in answering the raised question is how the concerned system performance can be quantitatively represented in terms of different delays in different channels. This is addressed by defining an error of the control signals involving the different delays in different channels. Based on this definition, the concerned question can then be formulated appropriately.

Consider the typical system setting of NCSs illustrated in Figure 1. Two delays exist in this system setting, i.e. the sensor-to-controller delay,  $\alpha$ , and the

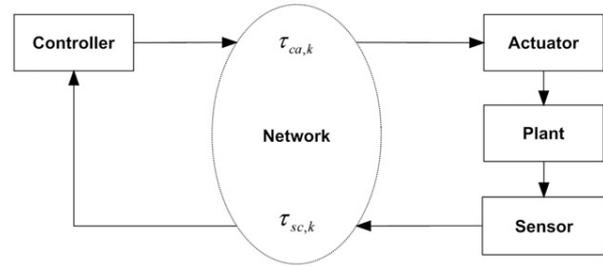


Figure 1. The block diagram of an NCS.

controller-to-actuator delay,  $\beta$ , respectively. We assume that the delays are upper bounded, i.e.

$$0 \leq \alpha \leq \bar{\tau}_{sc}, 0 \leq \beta \leq \bar{\tau}_{ca}, \quad (1)$$

and consequently,  $0 \leq \tau \leq \bar{\tau}$ .

In order to focus mainly on the delay effects rather than the plant dynamics, the following linear nominal system model for the plant is adopted:

$$x(k+1) = Ax(k) + Bu(k), \quad (2)$$

where  $x \in \mathbb{R}^n$ ,  $u \in \mathbb{R}^m$ ,  $A \in \mathbb{R}^{n \times n}$  and  $B \in \mathbb{R}^{n \times m}$ .

The following is an immediate observation from Figure 1, which however is the foundation of our analysis on the different delay effects in NCSs: it is the different control laws that may cause different delay effects in NCSs. More specifically, the delay effects on the evolution of the system in (2) entirely rely on how the control signal  $u(k)$  is obtained, as only  $u(k)$  is directly affected by the delays (this will be more evident afterwards when we categorise existing control laws). This observation enables us to focus mainly on the analysis of different control laws in NCSs.

Given a control law, define the difference of the control signals between the one with sensor-to-controller delay  $\alpha$  and controller-to-actuator delay  $\beta$  (denoted by  $u_\tau(k : \alpha, \beta)$ ) and the one without any delay (denoted by  $u_0(k)$ ), to be

$$e_\tau(k : \alpha, \beta) := |u_\tau(k : \alpha, \beta) - u_0(k)|. \quad (3)$$

Since  $u_0(k)$  is the control action achievable without any delay,  $e_\tau(k : \alpha, \beta)$  can thus be interpreted as a measure of how different delays in different channels would affect the ability of the system to achieve this desirable control action  $u_0(k)$ . Based on  $e_\tau(k : \alpha, \beta)$  we are able to give the index to evaluate the delay effects in different channels, as follows.

**Definition 2.1:** Given a control law (consequently the way of calculating the control signal  $u(k)$ ). The control law is said to be ‘different-channel-delay-independent’

(DCDI) if at any specific time  $k$ , for any fixed  $\tau$  and any combinations of  $\alpha$  and  $\beta$  satisfying  $\tau = \alpha + \beta$ ,

$$e_\tau(k : \alpha, \beta) = \text{constant.} \tag{4}$$

The control law is said to be ‘different-channel-delay-dependent’ (DCDD) otherwise. Furthermore, ‘the degree of the DCDD dependence’ is measured by  $e_\tau(k : \alpha, \beta)$ . For  $\tau = \alpha_1 + \beta_1 = \alpha_2 + \beta_2$  and  $\alpha_1 > \alpha_2$ , if

$$e_\tau(k : \alpha_1, \beta_1) > e_\tau(k : \alpha_2, \beta_2)$$

the sensor-to-controller delay  $\alpha$  is said to be affecting the system performance more severely, and vice versa.

Based on Definition 2.1, the general question raised in Section 1 can then be stated as: (1) Are all the control laws in NCSs DCDI? (2) If there exists a control law to be DCDD, then what is the degree of its DCDD dependence?

### 3. Categorising the control laws

It is realised that the system performance defined in Definition 2.1 is entirely dependent on the choice of the control laws. The existing control laws are therefore categorised as the necessary preparation for further analysis.

#### 3.1. Two general categories of the control laws

For simplicity of analysis, we concentrate merely on static state feedback for the system in (2). Two categories of control laws are observed, referred to as the ‘delay-independent’ and ‘delay-dependent’ control laws, respectively.

- Delay-independent control laws. This category of control laws can be seen in most conventional control methods, the general form of which can be written as follows:

$$u(k) = Kx(k - \tau), \tag{5a}$$

where  $K$  is the constant feedback gain and plenty of methods have been proposed to design it (Wang and Yang 2007; Gao et al. 2008; Xiong and Lam 2009). Although the control signal in (5a) is still dependent on the round trip delay  $\tau$ , the controller (feedback gain) is designed ‘independently’ from the delay.

- Delay-dependent control laws. A general form of the control laws belonging to this category can be written as follows:

$$u(k) = K_k x(k - \tau), \tag{5b}$$

where the feedback gain  $K_k$  is essentially time-varying and delay-dependent. Note that a specific delay-dependent control law may not be expressed explicitly in the form of (5b), i.e. the delay-dependent control law is defined in the ‘equivalent’ sense: whatever the specific form of a control law is, it is delay-dependent if and only if it is not delay-independent. See for example the control law in (9a) which is defined later.

#### 3.2. The delay-dependent control laws

The delay-dependent law given in (5b) is only of its general form. It can be implemented in practice via several different control strategies. In what follows the design framework of the packet-based control approach to NCSs is briefly introduced, which is one of the most important control strategies that can derive such a delay-dependent control law. This introduction then facilitates the categorisation of the delay-dependent control laws afterwards.

##### 3.2.1. How the delay-dependent control laws are designed: a packet-based control framework

The essential idea of packet-based control for NCSs is to take advantage of the fact that the data in NCSs is transmitted in the form of data packets via the communication network and, the packet size (denoted by  $B_p$ ) is often much larger than the data size required for encoding one single step of the control signal (denoted by  $B_c$ ). More precisely, the following relationship is held for most NCSs:

$$\bar{\tau} + 1 \leq \left\lfloor \frac{B_p}{B_c} \right\rfloor, \tag{6}$$

where  $\left\lfloor \frac{B_p}{B_c} \right\rfloor$  is the largest integer that is less than  $\frac{B_p}{B_c}$ .

The relationship in (6) implies that a sequence of the forward control signals, or referred to as the ‘forward control sequence’ (FCS), can be packed into one data packet and sent simultaneously to the actuator. The FCS is designed as follows if time-synchronisation is unavailable between the sensor and the controller,

$$U_N(k|k - \alpha) = [u(k - \alpha|k - \alpha) \dots u(k - \alpha + \bar{\tau}|k - \alpha)]. \tag{7}$$

In the presence of time-synchronisation between the sensor and the controller, the sensor-to-controller delay  $\alpha$  can be known by the controller (Zhao et al. 2009a). In this case the control signals from time  $k - \alpha$  to  $k - 1$  are clearly not necessary to be calculated as

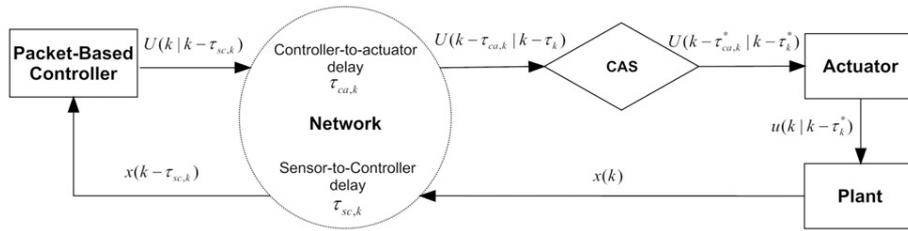


Figure 2. Packet-based control for NCSs.

they are impossible to be used at the actuator side. The above FCS can thus be shortened as follows:

$$U_S(k|k - \alpha) = [u(k|k - \alpha) \dots u(k + \bar{\tau}_{ca}|k - \alpha)], \quad (8)$$

where the control predictions in (7) and (8) are all calculated based on delayed sensing data at time  $k - \alpha$ . Notice that in the case of (7) the requirement in (6) can be relaxed by replacing  $\bar{\tau}$  by  $\bar{\tau}_{ca}$ . Notice also that in both (7) and (8)  $k$  refers to the time at the controller side.

By sending the FCSs simultaneously to the actuator and designing some auxiliary mechanisms (or control action selector) to choose from them the appropriate control signals, the communication constraints in NCSs including network-induced delay, data packet dropout and data packet disorder, can then be actively compensated for. The block diagram of a general packet-based (PBNCs) is illustrated in Figure 2. For more details of the packet-based control approach, the reader is referred to Zhao et al. (2008a,b, 2009a,b, 2010).

### 3.2.2. Categorising the delay-dependent control laws

The above design procedure of PBNCs provides only the control framework to compensate for the communication constraints in NCSs, whereas the design of the packet-based controller, or the FCS, can still be varied. In the early development of PBNCs (Liu et al. 2007), the controller is designed using a model-based control method. The idea is to first ‘estimate’, or ‘predict’ the current system state from the delayed sensing data and then use a constant feedback gain. We refer to this design method as the ‘prediction-based’ approach and the control law can be written as

$$u(k) = K\hat{x}(k|k - \tau), \quad (9a)$$

where  $\hat{x}(k|k - \tau)$  is the predicted state at time  $k$  based on the state at time  $k - \tau$ .

A recent development of PBNCs gives rise to a more flexible structure of PBNCs, where no

prediction of the system state is used, resulting in the following control law with the use of the FCS in (7),

$$u(k) = K_\tau x(k - \tau), \quad (9b)$$

where the feedback gain  $K_\tau$  is dependent on the round trip delay  $\tau$ . With the use of the FCS in (8), the control law is defined by

$$u(k) = K_{\alpha,\beta} x(k - \tau), \quad (9c)$$

where the feedback gain  $K_{\alpha,\beta}$  is dependent on both the sensor-to-controller delay,  $\alpha$  and the controller-to-actuator delay,  $\beta$ .

The most important feature of the control laws in (9b) and (9c) is that the feedback gains are now time-varying, i.e. we now have a set of feedback gains corresponding to different delays and at any specific time instant, a specific feedback gain is chosen from the set to reflect the current network condition. It thus brings more design freedom for the control engineers to compensate for the communication constraints in NCSs. A better system performance can therefore be expected (Zhao et al. 2009a).

**Remark 3.1:** Although the categorisation of the delay-dependent control laws are based on the packet-based control framework, it is necessary to point this out that this categorisation is widely applicable to almost all the delay-dependent control laws in NCSs. Therefore, the analysis that follows is actually in a very general sense.

## 4. When and how the delay effects in different channels are different

Based on the definition of the system performance index in Section 2 and the categorisation of existing control laws in NCSs in Section 3, we are now able to analyse the delay effects in different channels. A qualitative analysis is firstly conducted to clarify which categories of control laws are DCDD (DCDD)

and then a quantitative analysis is conducted for the DCDD control laws.

#### 4.1. When the delay effects are different: a qualitative analysis

A qualitative analysis of the delay-independent control law in (5a) and the delay-dependent control laws in (9a)–(9c) leads to the following proposition.

##### Proposition 4.1:

- (1) The delay-independent control law in (5a) and the delay-dependent control law in (9b) are DCDD.
- (2) The delay-dependent control laws in (9a) and (9c) are typically DCDD.

**Proof:** Notice that for any given  $k$  and  $\tau$ ,  $u_\tau(k : \alpha, \beta)$  remains to be constant for both control laws in (5a) and (9b). The first part of the proposition is thus correct by (3) and Definition 2.1.

As for the control law in (9c),  $u_\tau(k : \alpha, \beta)$  is varying with  $K_{\alpha, \beta}$  and is thus typically different for different combinations of  $\alpha$  and  $\beta$ , since otherwise, it degenerates to the control law in (9b).

The predicted system state in the control law in (9a) is usually designed based on a model of the plant. This design procedure presents two factors that would affect the predicted system state, that is, the model inaccuracy and the error occurred in the model prediction. The sensor-to-controller and the controller-to-actuator delays are related to these two factors in different ways (which will be more evident in the quantitative analysis in Section 4.2.1), meaning that these two delays typically present different delay effects for the system.  $\square$

**Remark 4.2:** As for the control law in (9a), it makes a difference in terms of the delay effects whenever a model-based controller is designed for the system. This means that besides the packet-based control approach, other model-based methods could also suffer from different delay effects for different sensor-to-control and controller-to-actuator delays, such as the approaches proposed in Montestruque and Antsaklis (2004). On the other hand, the idea of using delay-dependent feedback gains has also been seen in other models used for NCSs, see, e.g. Zhang, Shi, Chen, and Huang (2005), despite the missing of the practical design support. Clearly, the results obtained here and in what follows are also applicable to these models. This observation implies that the formulated problem and the obtained results are widely applicable to a large number of NCSs.

#### 4.2. How the delay effects with (9a) and (9c) are different: a quantitative analysis

The second part of Proposition 4.1, i.e. the different delay effects caused by the control laws in (9a) and (9c), are addressed quantitatively in this section. These obtained results provide important design principles for the practical implementation of NCSs.

##### 4.2.1. The prediction-based approach in (9a)

The design of the control law in (9a) can be various due to the different predictive methods used to obtain  $\hat{x}(k|k - \tau)$ . Examples of this variance can be seen in Liu et al. (2007) for a model-based approach and in Zhao et al. (2009a) for a receding horizon-based approach. In what follows a quantitative analysis is done for the case in Liu et al. (2007), whereas other cases can be analysed similarly.

The fundamental idea of predicting the state  $\hat{x}(k|k - \tau)$  in Liu et al. (2007) is to use an estimated plant model at the controller side, which can give the predicted states based on delayed state information. The model used can be written as

$$\hat{x}(k + 1) = \hat{A}\hat{x}(k) + \hat{B}\hat{u}(k), \quad (10)$$

where  $\hat{A}$  and  $\hat{B}$  are not equivalent to  $A$  and  $B$  in (2) in general due to the modelling error. Furthermore, the control signals  $\hat{u}(k)$  may not be the same as the real ones,  $u(k)$ , since the latter is usually not fully accessible to the controller.

Notice that  $k$  in (9a) is the time at the actuator side. The time when the FCS is calculated at the controller side is thus  $k - \beta$  and the FCS is calculated based on the delayed state information at time  $k - \tau$ . The prediction-based approach estimates the state  $\hat{x}(k|k - \tau)$  based on the available delayed state  $x(k - \tau)$ , using the following two steps.

- (1) Estimate from  $\hat{x}(k - \tau + 1|k - \tau)$  to  $\hat{x}(k - \beta|k - \tau)$ . In this step it is assumed that the real control signals applied to the plant from  $u(k - \tau)$  to  $u(k - \beta - 1)$  are available to the controller, that is,  $\hat{u}(k - \tau + i) = u(k - \tau + i)$ ,  $i = 0, 1, \dots, \beta + 1$ . It is realised later that this assumption is difficult to be implemented in practice and a better approach is proposed to deal with this difficulty (Zhao et al. 2008a). However in this article we keep this assumption unchanged for simplicity of analysis. Based on this assumption and the predictive model in (10), the dynamics of the predictive model can be written as

$$\begin{aligned} & \hat{x}(k - \tau + i|k - \tau) \\ &= \hat{A}\hat{x}(k - \tau + i - 1|k - \tau) \\ &+ \hat{B}u(k - \tau + i - 1), \quad i = 1, \dots, \alpha, \end{aligned} \quad (11)$$

where  $\hat{x}(k - \tau|k - \tau) = x(k - \tau)$ . This yields

$$\begin{aligned} & \hat{x}(k - \beta|k - \tau) \\ &= \hat{A}^\alpha x(k - \tau) + \sum_{j=1}^{\alpha} \hat{A}^{\alpha-j} \hat{B}u(k - \tau + j - 1). \end{aligned} \quad (12)$$

- (2) Estimate from  $\hat{x}(k - \beta + 1|k - \tau)$  to  $\hat{x}(k|k - \tau)$ . In this step the control signal is assumed to be given by  $\hat{u}(k - \beta + i) = u(k - \beta + i|k - \tau) = K\hat{x}(k - \beta + i|k - \tau)$ , as the real ones are clearly not available. Based on this assumption, the predictive model in (10) turns to be

$$\begin{aligned} & \hat{x}(k - \beta + i|k - \tau) \\ &= (\hat{A} + \hat{B}K)\hat{x}(k - \beta + i - 1|k - \tau), \\ & \quad i = 1, \dots, \beta, \end{aligned} \quad (13)$$

which gives

$$\hat{x}(k|k - \tau) = (\hat{A} + \hat{B}K)^\beta \hat{x}(k - \beta|k - \tau). \quad (14)$$

As state feedback with a constant feedback gain is used in (9a),  $e_\tau(k : \alpha, \beta)$  in (3) can thus be evaluated equivalently by the difference between the estimated state,  $\hat{x}(k|k - \tau)$  and the real one,  $x(k|k - \tau) = x(k)$ , i.e.

$$e(k|k - \tau) := x(k|k - \tau) - \hat{x}(k|k - \tau). \quad (15)$$

By (2)  $x(k|k - \tau)$  is given by

$$x(k|k - \tau) = A^\tau x(k - \tau) + \sum_{j=1}^{\tau} A^{\tau-j} Bu(k - \tau + j - 1), \quad (16)$$

which is based on the state at time  $k - \tau$ .

From (12), (14) and (16)  $e(k|k - \tau)$  can be explicitly expressed, which in general is a function of the sensor-to-controller delay,  $\alpha$ , (or the controller-to-actuator delay,  $\beta$ ) given the fixed round trip delay,  $\tau$ ,

$$e(k|k - \tau) = \Gamma_{\tau,K}(\alpha). \quad (17)$$

Although it is possible to investigate the explicit expression of  $e(k|k - \tau)$  in (17) directly, it is too complicated to derive any valuable results. As the main purpose of this article is to study the effects in the presence of different delays in different channels, it is thus possible to study the effects indirectly from two different dynamics of  $e(k|k - \tau)$ , based on (11) and (13). On the basis of this observation, the following result is obtained.

**Proposition 4.3:** *With the use of the prediction-based control law in Liu et al. (2007), the sensor-to-controller delay,  $\alpha$ , affects the system performance less than the controller-to-actuator delay,  $\beta$ , provided the predictive model in (10) is sufficiently precise.*

**Proof:** In order to demonstrate the above result, the error dynamics  $e(k|k - \tau)$  is analysed based on the aforementioned two steps in the prediction-based approach. From  $k - \tau$  to  $k - \beta$ , the error dynamics is obtained for  $i = 1, \dots, \alpha$ , as follows, based on (11) and (16),

$$\begin{aligned} e_\alpha(i) &:= e(k - \tau + i|k - \tau) \\ &= (A - \hat{A})x(k - \tau + i - 1|k - \tau) \\ &\quad + \hat{A}e(k - \tau + i - 1|k - \tau) \\ &\quad + (B - \hat{B})u(k - \tau + i - 1) \end{aligned} \quad (18)$$

with  $e(k - \tau|k - \tau) = 0$ .

On the other hand, from  $k - \beta + 1$  to  $k$ , the error dynamics is obtained for  $j = 1, \dots, \beta$ , based on (13) and (16), as follows:

$$\begin{aligned} e_\beta(j) &:= e(k - \beta + j|k - \tau) \\ &= (A - \hat{A} - \hat{B}K)x(k - \beta + j - 1|k - \tau) \\ &\quad + (\hat{A} + \hat{B}K)e(k - \beta + j - 1|k - \tau) \\ &\quad + Bu(k - \beta + j - 1). \end{aligned} \quad (19)$$

It is noticed that the error  $e_\alpha(\cdot)$  is purely dependent on the sensor-to-controller delay,  $\alpha$ , and is accumulated with the increase of  $\alpha$ . On the other hand, although  $e_\beta(\cdot)$  is mainly affected by the controller-to-actuator delay, it is also affected by the sensor-to-controller delay, since its initial state,  $e(k - \beta|k - \tau)$ , is obtained in (18).

Now suppose we have an exact model of the plant, i.e.  $A = \hat{A}$ ,  $B = \hat{B}$ . It immediately follows that  $e_\alpha(i) \equiv 0$ ,  $i = 1, \dots, \alpha$ , and in particular the initial state for (19),  $e(k - \beta|k - \tau) = e_\alpha(\alpha) = 0$ . Therefore, in this case the sensor-to-controller delay does not affect the system performance at all. On the other hand, it is readily seen that  $e_\beta(i) \neq 0$  in general and will accumulate with the increase of  $\beta$ . Based on this observation, it is therefore fair to claim the statement made in this proposition.  $\square$

**Remark 4.4:** Proposition 4.3 implies that, under certain conditions, it can result in a better system performance to place the controller as close to the actuator as possible, if the system allows us to do so. In this sense Proposition 4.3 has its practical guidance value. However, Proposition 4.3 is based on the nominal system and it could be wrong in the presence of large model inaccuracy, measurement error or any other type of uncertainties in the system. Indeed, as stated in the proof, the sensor-to-controller delay affects both  $e_\alpha(\cdot)$  and  $e_\beta(\cdot)$  while the controller-to-actuator delay affects only  $e_\beta(\cdot)$ . Therefore, if the system setting allows the sensor-to-controller delay to take effect, it is very likely that this delay could affect

the system performance more severely than that of the controller-to-actuator delay. This implies that Proposition 4.3 has its rigid conditions of applicability.

4.2.2. *The delay-dependent gain based approach in (9c)*

Unlike the prediction-based approach in (9a) where the prediction of the current system state plays an essential role, the delay effects in the delay-dependent gain based approach in (9c) are purely dependent on the time-varying feedback gains. In order to specify  $e_\tau(k: \alpha, \beta)$  in (3), we consider, for given round trip delay,  $\tau$ , the unit error with respect to the delay in the sensor-to-controller channel,  $\alpha$ ,

$$\Delta e_\alpha := \|K_{\alpha+1, \beta-1} - K_{\alpha, \beta}\| \|x(k - \tau)\| = \Delta K_\alpha \|x(k - \tau)\|, \tag{20}$$

and the unit error with respect to the delay in the controller-to-actuator channel,  $\beta$ ,

$$\Delta e_\beta := \|K_{\alpha-1, \beta+1} - K_{\alpha, \beta}\| \|x(k - \tau)\| = \Delta K_\beta \|x(k - \tau)\|, \tag{21}$$

where  $\|\cdot\|$  is the norm of  $\cdot$ ,  $\Delta K_\alpha = \|K_{\alpha+1, \beta-1} - K_{\alpha, \beta}\|$  and  $\Delta K_\beta = \|K_{\alpha-1, \beta+1} - K_{\alpha, \beta}\|$ .

Recalling (9c), it is noticed that  $K_{\alpha, \beta}x(k - \tau) = u(k)$  is the control signal actually applied to the plant at time  $k$ .  $\Delta e_\alpha$  ( $\Delta e_\beta$ ) can thus be interpreted as the difference between  $u(k)$  and the control signal produced by increasing (decreasing) a unit delay in the sensor-to-controller channel and meanwhile decreasing (increasing) a unit delay in the controller-to-actuator channel. Therefore, to a certain extent  $\Delta e_\alpha$  ( $\Delta e_\beta$ ) is able to quantitatively measure the delay effects in the sensor-to-controller (controller-to-actuator) channel: the larger  $\Delta e_\alpha$  ( $\Delta e_\beta$ ) is, the more the delay in the sensor-to-controller (controller-to-actuator) channel affects the system performance. This fact is stated in the following proposition.

**Proposition 4.5:** *In the delay-dependent gain-based approach in (9c), the effects of the delays in the sensor-to-controller channel and the controller-to-actuator channel are proportional to  $\Delta K_\alpha$  and  $\Delta K_\beta$ , respectively.*

**Remark 4.6:** Notice that for the control law in (9b), for any given round trip delay the feedback gain remains fixed. This implies that for any given round trip delay,  $\tau$ ,

$$K_\tau = K_{\alpha+1, \beta-1} = K_{\alpha-1, \beta+1}, \quad \forall \alpha + \beta = \tau.$$

Therefore, in a certain sense the delay effects of the control law in (9b) can be deduced from Proposition 4.5.

**Remark 4.7:** It can be often seen in practice that either  $\Delta K_\alpha > \Delta K_\beta$  or  $\Delta K_\alpha < \Delta K_\beta$  is met by almost all round trip delays with only a few exceptions. In this case we should be confident to conclude that the sensor-to-controller delay or the controller-to-actuator delay plays more essential role than its counterpart although this conclusion cannot be obtained directly from Proposition 4.5. In this sense the conditions in Proposition 4.5 can be too rigid to be actually applied in practice. To deal with this issue, we define the following global gain error,  $K_\alpha$  and  $K_\beta$ , based on the partial gain error,  $\Delta K_\alpha$  and  $\Delta K_\beta$ , respectively,

$$K_\alpha := \sum_{\tau} \sum_{\alpha+\beta=\tau} \Delta K_\alpha, \tag{22}$$

$$K_\beta := \sum_{\tau} \sum_{\alpha+\beta=\tau} \Delta K_\beta. \tag{23}$$

It is seen that  $K_\alpha$  and  $K_\beta$  are the sum of  $\Delta K_\alpha$  and  $\Delta K_\beta$  over all possible delays. Therefore, the former can be an effective measure for the delay effects in a global sense. Proposition 4.5 can also be modified accordingly to represent this global measure.

**Remark 4.8:** Proposition 4.5 has its guidance value in the practical implementation of NCSs. After the feedback gains in (9c) have been designed,  $\Delta K_\alpha$  and  $\Delta K_\beta$  in (20) and (21), and consequently the different delay effects, can then be determined by Proposition 4.5. The practical implementation can then be adjusted accordingly in favour of the system performance.

4.3. *A brief summary and discussion*

We are now able to summarise the points scattered all over this article on the different delay effects in NCSs in Table 1.

Table 1 tells us that if the controller in a specific NCS is designed using a control law belonging to the controller category in (5a) or (9b), the sensor-to-controller and the controller-to-actuator delays are identical in terms of their effects on the system performance; however, if otherwise the control law belongs to the controller category in (9a) or (9c), the sensor-to-controller and the controller-to-actuator delays can possibly affect the system performance in different ways. As regards the practical implementing, we may therefore try to decrease as much as possible the delay which deteriorates the system performance more if the system allows us to do so. This can be served as an important design principle in the implementation of any NCSs.

Table 1. The different delay effects in NCSs.

Controller category	Which delay more affects the performance?	Implementation considerations
(5a) and (9b)	No difference <sup>a</sup>	NA
(9a)	The controller-to-actuator delay <sup>b</sup>	Minimise the controller-to-actuator delay <sup>c</sup>
(9c)	Dependent on different controller gains <sup>d</sup>	Adjust the control structure accordingly <sup>e</sup>

Notes: <sup>a</sup>Proposition 4.1.

<sup>b</sup>Proposition 4.3.

<sup>c</sup>Remark 4.4.

<sup>d</sup>Proposition 4.5 and Remark 4.7.

<sup>e</sup>Remark 4.8.

## 5. Numerical examples

Two numerical examples are considered to verify the conclusions made in the previous section, regarding the delay effects of the prediction-based approach (Example 5.1) and the delay-dependent gain based approach (Example 5.2), respectively. All the simulations that follow are done using MATLAB.

**Example 5.1:** Consider the system in (2) with the following system matrices borrowed from Liu et al. (2007),

$$A = \begin{pmatrix} 1.010 & 0.271 & -0.488 \\ 0.482 & 0.100 & 0.240 \\ 0.002 & 0.3681 & 0.7070 \end{pmatrix}, \quad B = \begin{pmatrix} 5 & 5 \\ 3 & -2 \\ 5 & 4 \end{pmatrix}.$$

As in Liu et al. (2007), the initial state is set as  $x_0 = [0.1 \ 0.1 \ 0.1]^T$  and the constant feedback gain is given by

$$K = \begin{pmatrix} 0.5858 & -0.1347 & -0.4543 \\ -0.5550 & 0.0461 & 0.4721 \end{pmatrix}.$$

Different from the system setting in Liu et al. (2007), it is assumed that the system states of the above system can be obtained exactly and therefore the measurement system and the observer are not necessary. The control signal is assumed to be zero before the arrival of the first FCS. In addition, in order to focus on the delay effects in different channels, the delays are all set to be time-invariant.

The simulations of the above system prove the statement made in Proposition 4.3 and Remark 4.4. Under the same round trip delay,  $\bar{\tau} = 3$ , Figure 3 shows that the system is stable with  $\tau_{ca} = 1$  while unstable with  $\tau_{ca} = 2$ . This proves the result in Proposition 4.3, that is, the smaller the controller-to-actuator delay is, the better the system performance will be. Further examples can be seen in Figures 4 and 5. With  $\tau_{ca} = 1$  and  $\tau_{sc} = 1$  respectively, the system is stable even with  $\tau_{sc} = 12$  (Figure 4) while only stable for  $\tau_{ca} < 2$  (Figure 5). This clearly shows that the sensor-to-controller delay has a less negative effect on

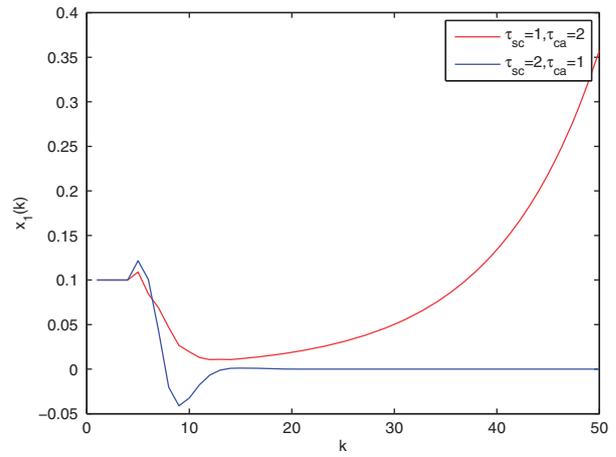


Figure 3. Example 1: state responses with different delays in different channels.

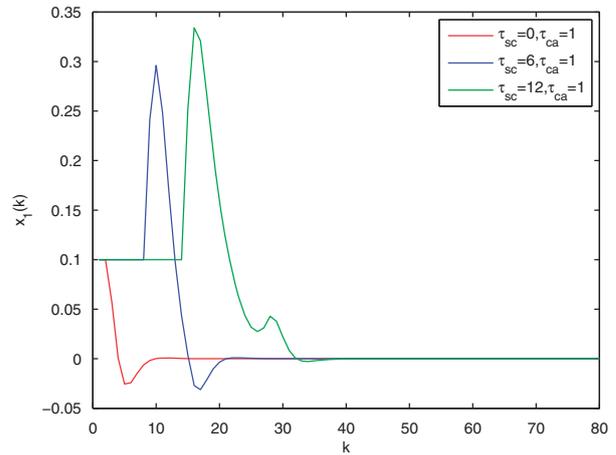


Figure 4. Example 1: state responses with the same controller-to-actuator delay.

the system performance. In order to simulate the delay effects in the presence of the modelling error, a particular case is shown in Figure 6, where the inaccurate system matrices are defined as

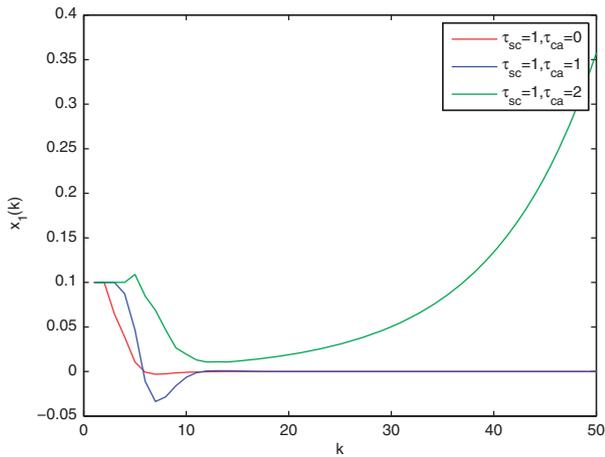


Figure 5. Example 1: state responses with the same sensor-to-controller delay.

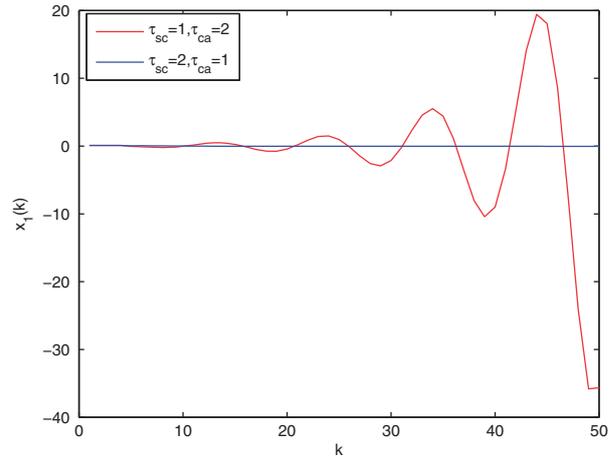


Figure 7. Example 2: state responses with different delays in different channels.

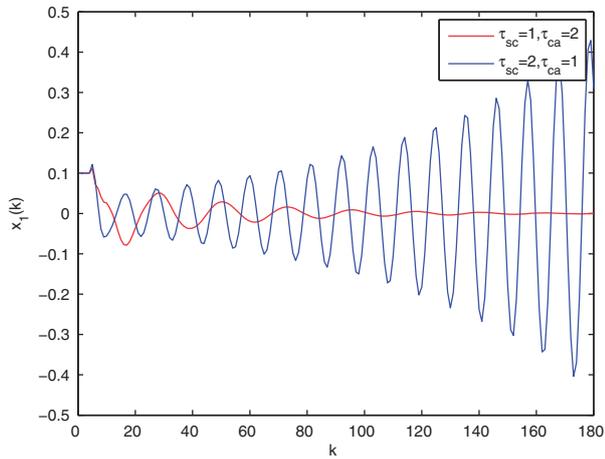


Figure 6. Example 1: state responses in the presence of modelling error.

$\hat{A} = (1 + \epsilon)A$  and  $\hat{B} = (1 - \epsilon)B$  with  $\epsilon = 0.16$ . For this particular case it shows that the sensor-to-actuator delay could affect the system performance more severely. This proves the statement made in Remark 4.4. However, it is worth pointing out that with inaccurate models, the sensor-to-actuator delay could still be possible to affect the system performance more lightly. This implies that with the modelling error in presence, the delay effects in different channels are complicated and no general results exist.

**Example 5.2:** Consider the same system as in Example 5.1 but with the control law in (9c). In order to consider the different delay effects in this case, we redefine the upper bounds of the delay as  $\bar{\tau}_{sc} = \bar{\tau}_{ca} = 2$  and thus  $\bar{\tau} = 4$ . The delay-dependent

feedback gains are then designed based on a receding horizon approach, as proposed in Zhao et al. (2009a),

$$\begin{pmatrix} K_{0,0} \\ K_{0,1} \\ K_{0,2} \end{pmatrix} = \begin{pmatrix} -0.0312 & -0.0822 & -0.1719 \\ -0.1446 & 0.0568 & 0.2801 \\ 0.0583 & -0.0172 & -0.0976 \\ -0.1591 & 0.0427 & 0.2559 \\ 0.0474 & -0.0128 & -0.0765 \\ -0.1253 & 0.0338 & 0.2020 \end{pmatrix},$$

$$\begin{pmatrix} K_{1,0} \\ K_{1,1} \\ K_{1,2} \end{pmatrix} = \begin{pmatrix} -0.1333 & 0.0018 & 0.1319 \\ -0.0772 & 0.0191 & 0.1235 \\ 0.0085 & -0.0027 & -0.0147 \\ -0.0290 & 0.0073 & 0.0455 \\ 0.0087 & -0.0022 & -0.0137 \\ -0.0230 & 0.0059 & 0.0363 \end{pmatrix}.$$

$$\begin{pmatrix} K_{2,0} \\ K_{2,1} \\ K_{2,2} \end{pmatrix} = \begin{pmatrix} -0.1629 & 0.0137 & 0.1890 \\ -0.0256 & 0.0053 & 0.0405 \\ 0.0010 & -0.0006 & -0.0024 \\ -0.0104 & 0.0022 & 0.0152 \\ 0.0030 & -0.0006 & -0.0045 \\ -0.0081 & 0.0017 & 0.0120 \end{pmatrix}.$$

As for the above delay-dependent gains, there is no general conclusion whether  $\Delta K_\alpha > \Delta K_\beta$  or  $\Delta K_\alpha < \Delta K_\beta$ . The global gain error is then calculated by (22), which turns to be  $K_\alpha = 0.0763$  and  $K_\beta = 0.1688$ . This indicates that in general the controller-to-actuator delay,  $\beta$ , affects the system performance more than the sensor-to-controller delay,  $\alpha$ . This conclusion is verified by the state responses shown in Figure 7, where the increase of the controller-to-actuator delay rapidly destabilises

the system, showing the more important role played by the controller-to-actuator delay.

## 6. Conclusions

Delays play an important role in NCSs. It is revealed for the first time that delays in different channels can possibly affect the system performance in very different ways. By categorising existing control laws, qualitatively and quantitatively analysing their roles in determining the delay effects in different channels, conditions and criteria are given to determine which delay can be more important under various conditions. These results can serve as important design principles in the practical implementation of NCSs.

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## 1. On the delay effects of different channels in Internet-based networked control systems

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